

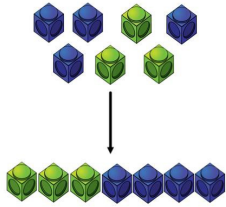
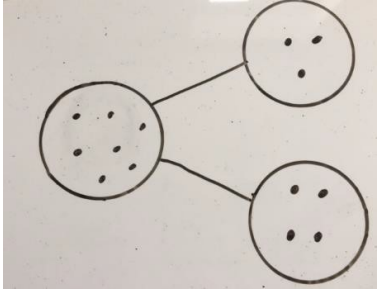
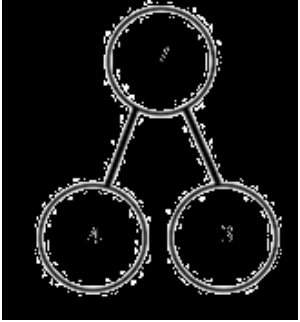
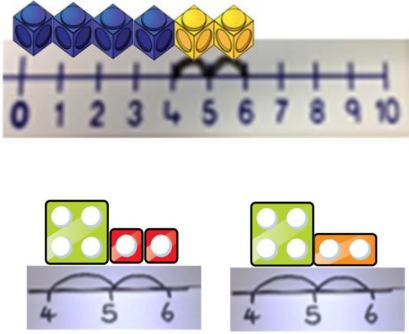
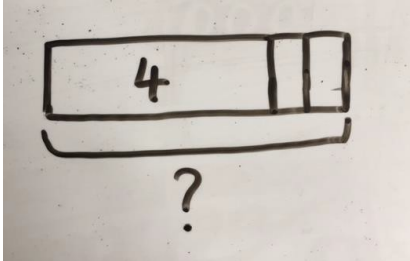

East Stanley School



Calculation Policy

Addition

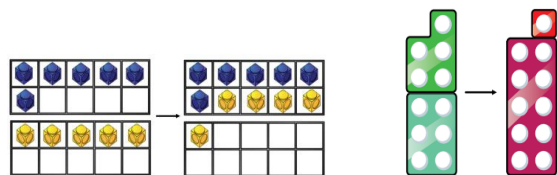
Key Vocabulary: *sum, total, altogether, plus, add, more, part, whole, is equal to, is the same as.*

Concrete	Pictorial	Abstract
<p>Combining two parts to make a whole using a variety of concrete resources:</p> 	<p>Children to represent the objects using dots or crosses on a part-whole model:</p> 	<p>$4+3=7$ Four is a part, 3 is a part and the whole is 7:</p> 
<p>Counting on using number lines using cubes or Numicon:</p> 	<p>Use of a bar model to encourage children to count on:</p> 	<p>The abstract number line:</p> <p>What is 2 more than 4?</p> <p>What is the sum of 2 and 4?</p> <p>What is the total of 4 and 2?</p> <p>$4+2=6$</p> 

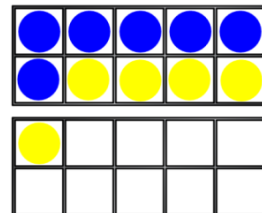
Regrouping to make 10 using 10s frames and counters or using

Numicon:

$$6+5$$



Children draw 10s frame and counters:



Children to develop an understanding of equality:

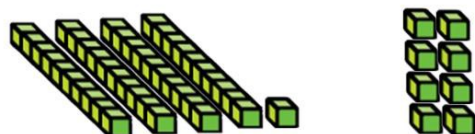
$$6+* = 11$$

$$6+5 = 5+6$$

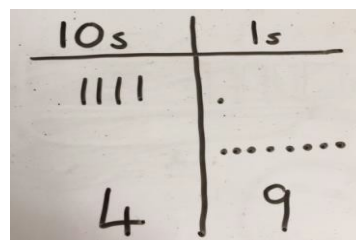
$$6+5 = *+4$$

TO+O using base 10.

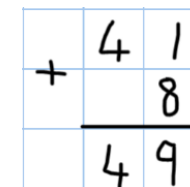
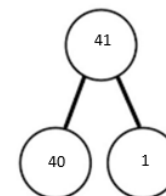
Develop understanding of partitioning and place value:



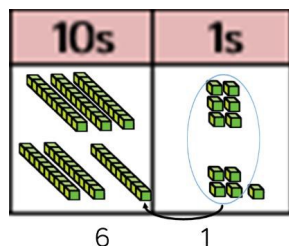
Represent the base 10 pictorially e.g.



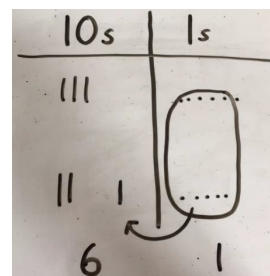
$$41+8$$



TO+TO using base 10. Continue to develop understanding of partitioning and place value. $36+25$



Represent the base 10 pictorially:



Looking for ways to make 10:

$$36 + 25 = 30+20=50$$

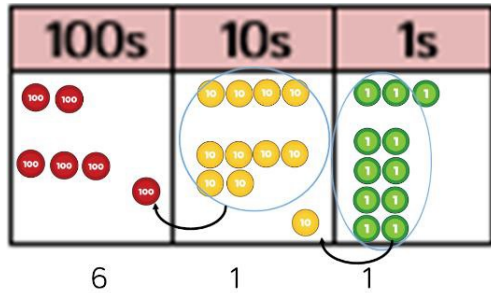
$$5+5=10$$

$$50+10+1=61$$

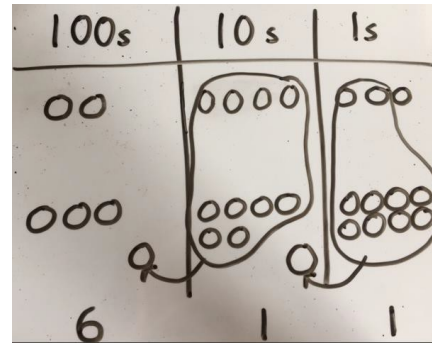
Leading to formal method:

$$\begin{array}{r} 36 \\ +25 \\ \hline 61 \\ \hline 1 \end{array}$$

Use of place value counters to add.
When there are 10 1s we exchange for 1 10. When there are 10 10s we exchange for 1 100.



Children to represent the counters in a place value chart, circling when they make an exchange.



Standard written method

$$\begin{array}{r} 243 \\ +368 \\ \hline 611 \\ \hline 11 \end{array}$$

Conceptual variation; different ways to ask children to solve 21+34

Word Problems:
In Y3 there are 21 children and in Y4 there are 34 children.

How many children in total?

$$21 + 34 = 55$$

Prove it.

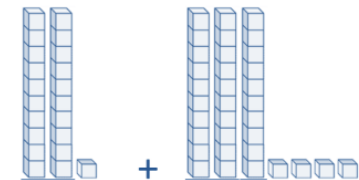
?	
21	34

$$21 + 34 = 55$$

$$\square = 21 + 34$$

Calculate the sum of 21 and 34.

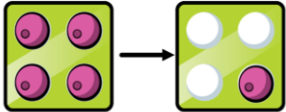
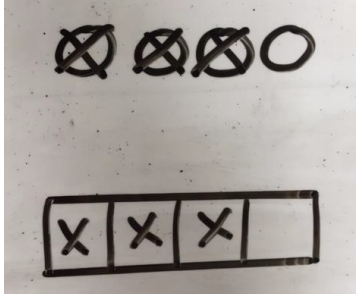
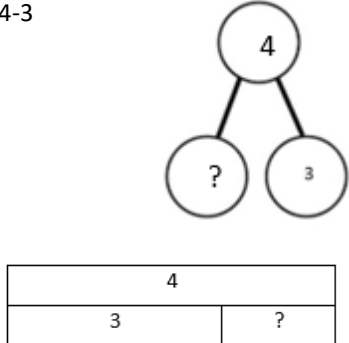
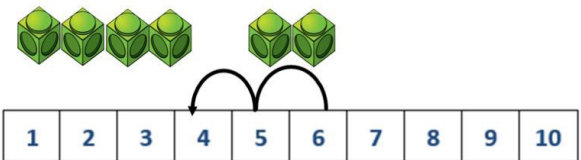
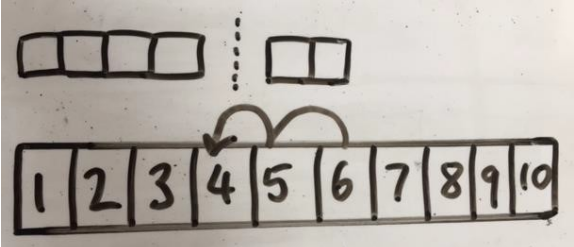
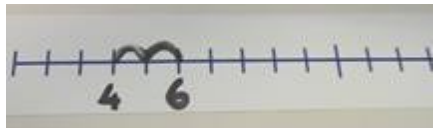
$$\begin{array}{r} 21 \\ +34 \\ \hline \hline \end{array}$$



10s	1s
10 10	1
10 10 10	?
?	5

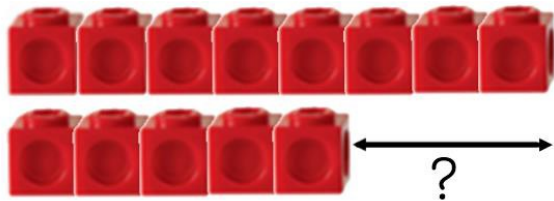
Subtraction

Key Vocabulary: take away, less than, the difference, subtract, minus, fewer, decrease.

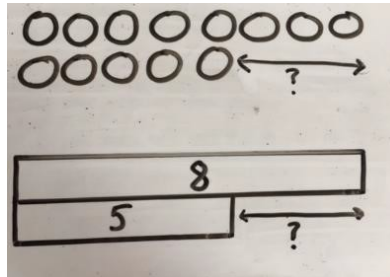
Concrete	Pictorial	Abstract
<p>Physically taking and removing objects from a whole.</p> <p>$4-3=1$</p> 	<p>Children to draw the resources they are using and cross them out. The bar model can also be used.</p> 	<p>$4-3 =$ $\square = 4-3$</p> 
<p>Counting back using number lines.</p> <p>Children start at 6 and count back 2.</p> <p>$6-2=4$</p> 	<p>Children to represent what they see pictorially.</p> 	<p>Children to represent the calculation on a number line and show their jumps. Use an empty number line.</p> 

Finding the difference using cubes, Numicon or other objects.

Find the difference between 8 and 5.



Children to draw what they have used or use the bar model to illustrate the calculation.



Find the difference between 8 and 5.

8-5, the difference is \square

Children to explore why:

8-5

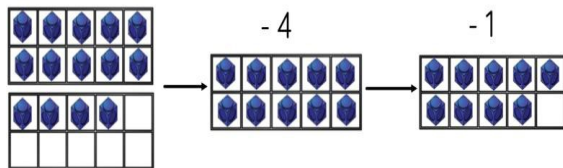
9-6

7-4

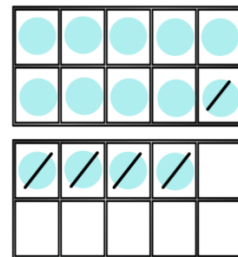
have the same answer.

Using 10 frames;

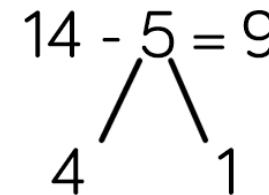
14-5



Children to represent the 10s frame pictorially.



Children partition the subtrahend.

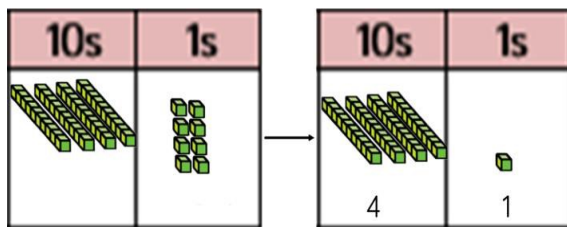


14-4=10

10-1=9

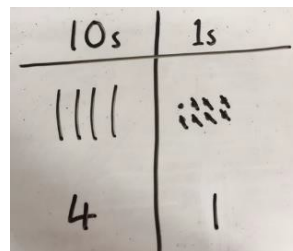
Column method using base 10.

48-7

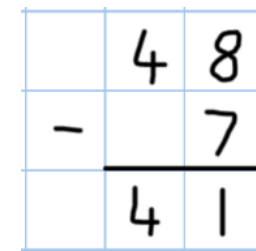


Children to represent the base 10

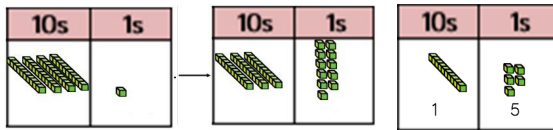
Pictorially.



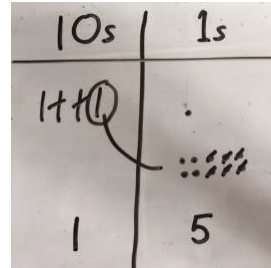
Column method or count back 7.



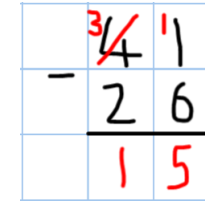
Column method using base 10 and having to exchange.
41-26



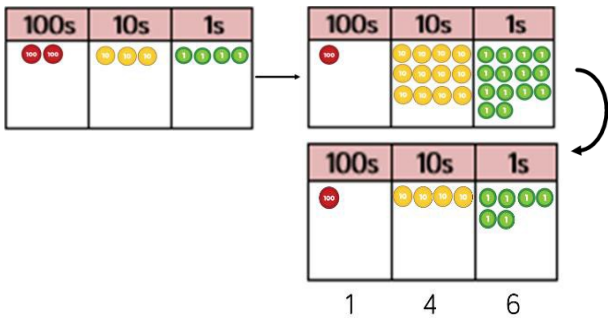
Represent the base 10 pictorially, remembering to show the exchange.



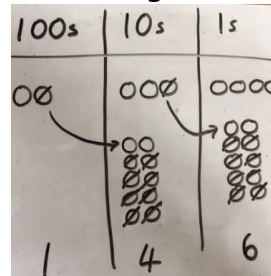
Formal column method. Children must understand that when they have exchanged the 10 they still have 41 because $41 = 31 + 11$.



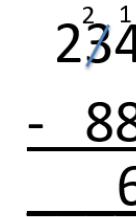
Column method using place value Counters. 234-88



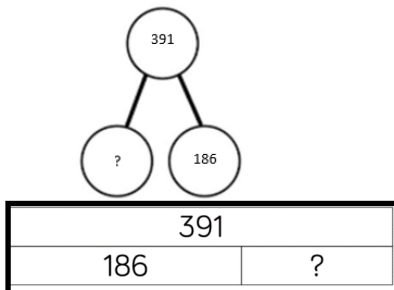
Represent the place value counters pictorially, remembering to show what has been exchanged.



Formal column method. Children must understand when they have crossed out the digits.



Conceptual variation; different ways to ask children to solve 391-186.



Raj spent £391 Tim spent £186. How much more did Raj spend?

Calculate the difference between £391 and £186.

$\square = 391 - 186$

$$\begin{array}{r} 391 \\ - 186 \\ \hline \end{array}$$

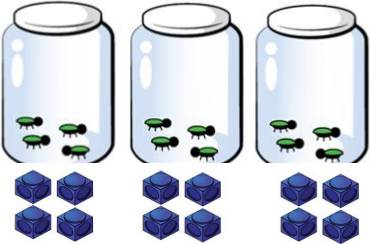
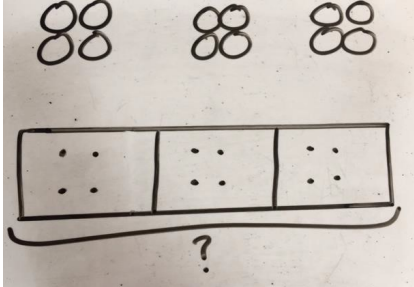
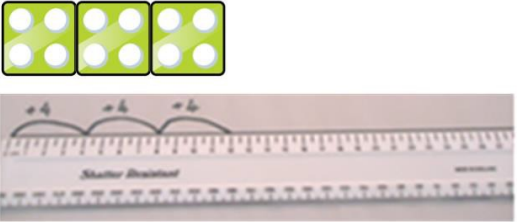
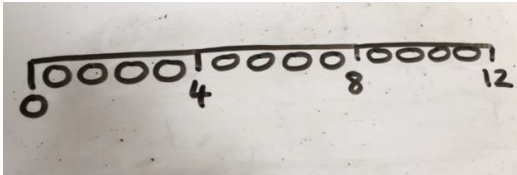
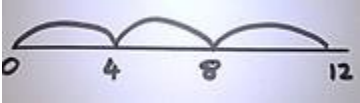
What is 186 less than 391?

Missing digit calculations.

$$\begin{array}{r} 39\square \\ - \square\square 6 \\ \hline \square 0 5 \end{array}$$

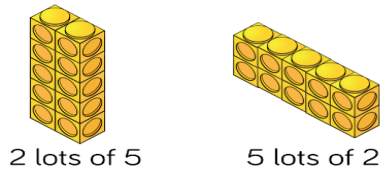
Multiplication

Key Vocabulary: *double, times, multiplied by, the product of, groups of, lots of, equal groups.*

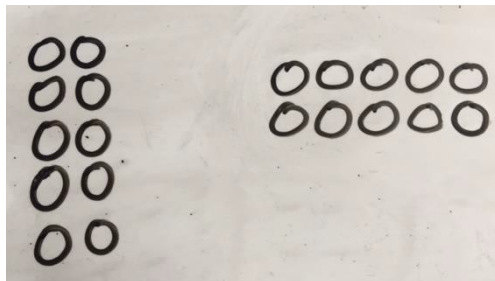
Concrete	Pictorial	Abstract
<p>Repeated grouping/repeated addition 3×4 $4+4+4$</p> <p>There are 3 equal groups with 4 in each group.</p> 	<p>Children to represent the concrete resources pictorially and use a bar model.</p> 	<p>$3 \times 4 = 12$ $4 + 4 + 4 = 12$</p>
<p>Number lines to show repeated groups. 3×4</p>  <p>Cuisenaire rods can be used too.</p>	<p>Represent this pictorially alongside a number line e.g.</p> 	<p>Abstract number line showing three jumps of four: $3 \times 4 = 12$</p> 

Use arrays to demonstrate commutativity. Counters and other Objects can be used.

$$2 \times 5 = 5 \times 2$$



Children to represent arrays Pictorially.



Children to use an array to write a range of calculations e.g.

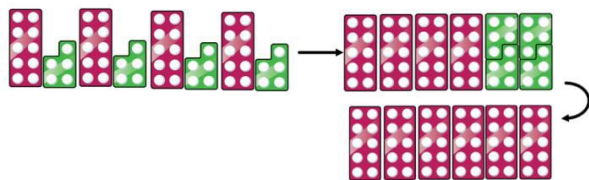
$$10 = 2 \times 5$$

$$5 \times 2 = 10$$

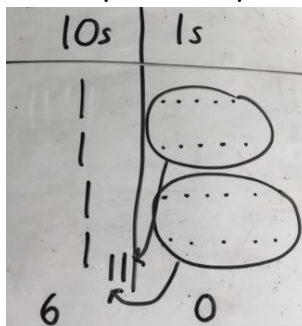
$$2 + 2 + 2 + 2 + 2 = 10$$

$$10 = 5 + 5$$

Partition to multiply using Numicon, Base 10 or Cuisenaire rods:
 4×15



Children to represent the concrete manipulatives pictorially.



Children to be encouraged to show the steps they have taken.

$$4 \times 15$$

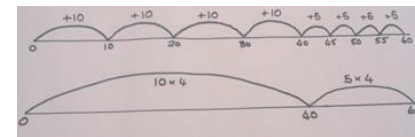
$$\swarrow \searrow$$

$$10 \quad 5$$

$$10 \times 4 = 40$$

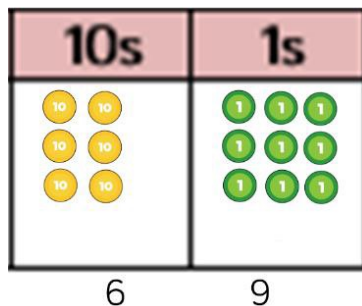
$$5 \times 4 = 20$$

$$40 + 20 = 60$$

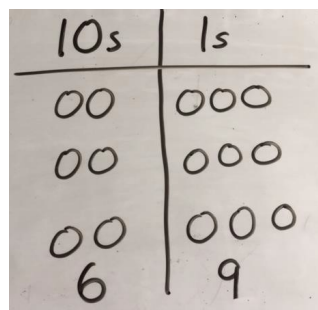


A number line can also be used.

Formal column method with place value Counters (base 10 can also be used).
 3×23



Children to represent the counters pictorially.



Children to demonstrate what it is they are doing to show understanding.

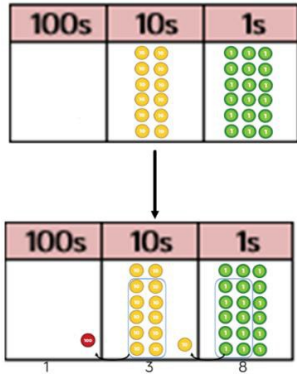
$$3 \times 20 = 60$$

$$3 \times 3 = 9$$

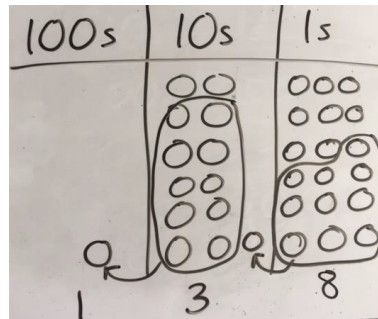
$$60 + 9 = 69$$

$$\begin{array}{r} 23 \\ \times 3 \\ \hline 69 \end{array}$$

Formal column method with place value counters.



Represent the place value counters/ base ten pictorially.



Formal written method.

$$6 \times 23 =$$

$$\begin{array}{r} 23 \\ \times 6 \\ \hline 138 \\ 11 \end{array}$$

When children start to multiply 3 digit numbers by 3 digit numbers and 4 digit numbers by 2 digit numbers they should be confident with the abstract.

$$\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 480 \\ \hline 3224 \\ 11 \end{array}$$

Answer: 3224

Conceptual variation; different ways to ask children to solve 6×23

23	23	23	23	23	23
----	----	----	----	----	----

?

Maia had to swim 23 lengths 6 times a week. How many lengths did she swim in 1 week?

With counters, prove $6 \times 23 = 138$

Find the product of 6 and 23

$$6 \times 23 =$$

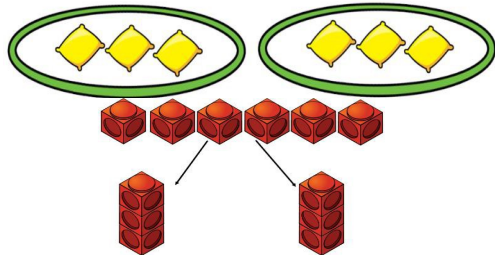
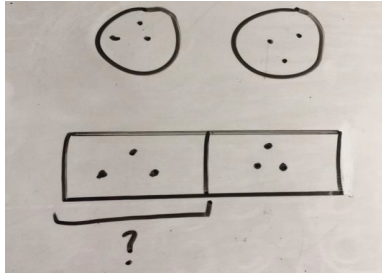

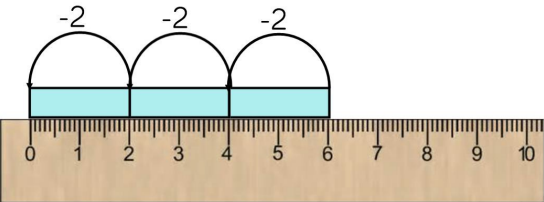
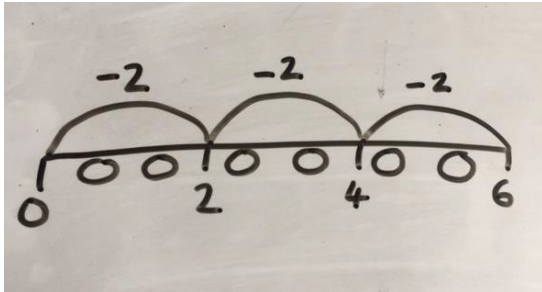
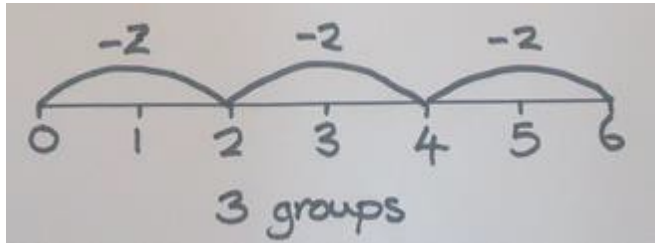
$$\square = 6 \times 23$$

What is the calculation?
What is the product?



Division

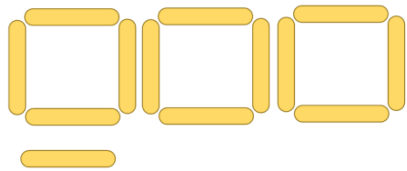
Key Vocabulary: *share, group, divide, divided by, half.*

Concrete	Pictorial	Abstract
<p>Sharing objects using a range of objects $6 \div 2$</p> 	<p>Represent the sharing pictorially.</p> 	<p>$6 \div 2 = 3$</p>  <p>Children should also be encouraged to use their 2 times table facts.</p>
<p>Repeated subtraction using Cuisenaire rods above a ruler $6 \div 2$</p>  <p style="text-align: center;">3 groups of 2</p>	<p>Children to represent repeated subtraction pictorially.</p> 	<p>Abstract number line to represent the equal groups that have been subtracted.</p> 

2 digit number divided by 1 digit number

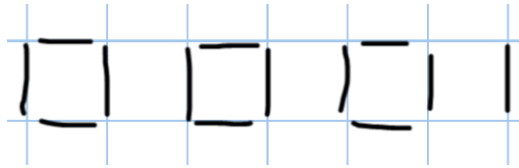
$$13 \div 4$$

Use of lollipop sticks to form wholes—squares because we are Dividing by 4.



There are 3 whole squares, with 1 left over.

Children to represent lollipop sticks pictorially.

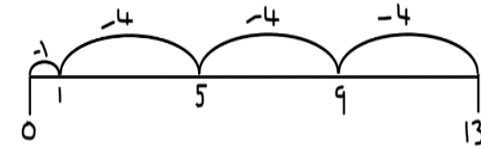


There are 3 whole squares, with 1 left over.

$$13 \div 4 = 3 \text{ remainder } 1$$

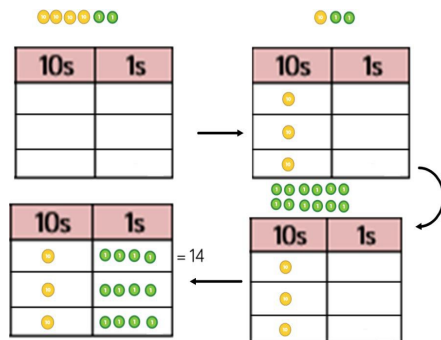
Children should be encouraged to use times table facts; they could also represent repeated subtraction on a number line:

3 groups of 4 with 1 left over

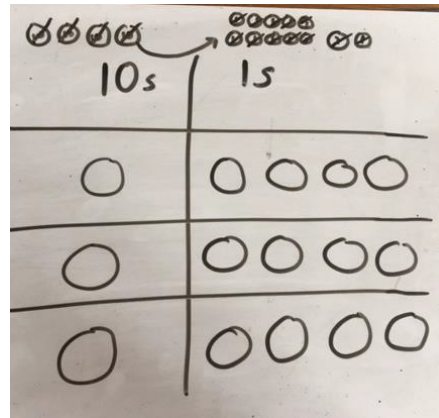


Sharing using place value counters:

$$42 \div 3 = 14$$



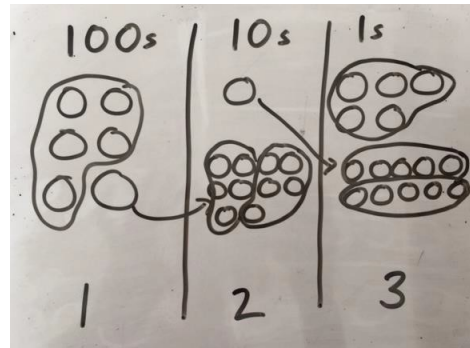
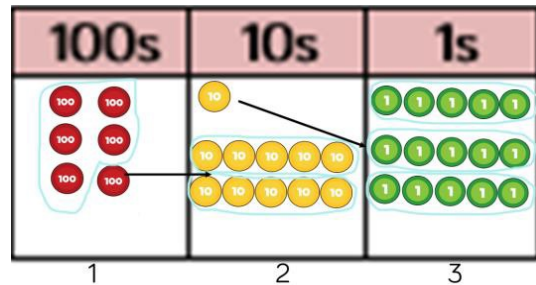
Children to represent the place value counters pictorially.



Children to make sense of the place value counters and write calculations to show the process:

$$\begin{aligned} 42 \div 3 \\ 42 &= 30 + 12 \\ 30 \div 3 &= 10 \\ 12 \div 3 &= 4 \\ 10 + 4 &= 14 \end{aligned}$$

Short division using place value counters to group:
 $615 \div 5$

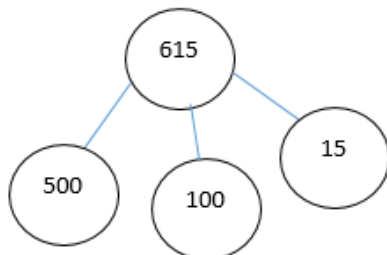


$$\begin{array}{r} 123 \\ 5 \overline{) 615} \\ \underline{5} \\ 11 \\ \underline{10} \\ 15 \\ \underline{15} \\ 0 \end{array}$$

Division by a two digit divisor using the above method.

Conceptual Variation; different ways to ask children to solve $615 \div 5$

Using the part whole model below, how can you divide 615 by 5 without using division.



I have £615 and share it equally between 5 bank accounts. How much will be in each account?

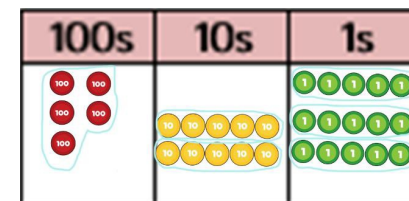
615 pupils need to be put into 5 groups. How many will be in each group?

$$615 \div 5 =$$

$$\square = 615 \div 5$$

What is the calculation?

What is the answer?



Calculation Policy: Guidance

	EYFS/Y1	Y2	Y3	Y4	Y5	Y6
Addition	<p>Combining two parts to make a whole: part whole model.</p> <p>Starting at the bigger number and counting on - using cubes.</p> <p>Regrouping to make 10 using ten frame.</p>	<p>Adding three single digits.</p> <p>Use of base 10 to combine two Numbers (up to two 2-digit numbers).</p>	<p>Column method - regrouping.</p> <p>Using place value counters (up to 3 digits).</p>	<p>Column method - regrouping. (up to 4 digits—to include up to two decimal places in context of money).</p>	<p>Column method - regrouping.</p> <p>Use of place value counters for adding decimals.</p>	<p>Column method- regrouping.</p> <p>Abstract methods.</p> <p>Place value counters to be used for adding decimal numbers.</p>
Subtraction	<p>Taking away ones</p> <p>Counting back</p> <p>Find the difference</p> <p>Part whole model</p> <p>Make 10 using the ten frame .</p>	<p>Counting back</p> <p>Find the difference</p> <p>Part whole model</p> <p>Make 10</p> <p>Use of base 10</p>	<p>Column method with regrouping.</p> <p>(up to 3 digits using place value counters)</p>	<p>Column method with regrouping.</p> <p>(up to 4 digits)</p>	<p>Column method with regrouping.</p> <p>Abstract for whole numbers.</p> <p>Start with place value counters for decimals- with the same amount of decimal places.</p>	<p>Column method with regrouping.</p> <p>Abstract methods.</p> <p>Place value counters for decimals- with different amounts of decimal places.</p>

	EYFS/Y1	Y2	Y3	Y4	Y5	Y6
Multiplication	<p>Recognising and making equal groups.</p> <p>Doubling</p> <p>Counting in multiples</p> <p>Use cubes, Numicon and other objects in the classroom .</p>	<p>Arrays- showing commutative multiplication.</p>	<p>Arrays- 2digit \times 1digit using base 10</p>	<p>Column multiplication- introduced with place value counters.</p> <p>(2 and 3 digit multiplied by 1 digit)</p>	<p>Column multiplication</p> <p>Abstract only but might need a repeat of year 4 first (up to 4 digit numbers multiplied by 1 or 2 digits)</p>	<p>Column multiplication</p> <p>Abstract methods (multi-digit up to 4 digits by a 2 digit number)</p>
Division	<p>Sharing objects into groups</p> <p>Division as grouping e.g. I have 12 sweets and put them in groups of 3, how many groups?</p> <p>Use cubes and draw round 3 cubes at a time.</p>	<p>Division as grouping</p> <p>Division within arrays- linking to multiplication</p> <p>Repeated subtraction</p>	<p>Division with a remainder- using lollipop sticks, times tables facts and repeated subtraction.</p> <p>2digit divided by 1digit using base 10 or place value counters leading to Standard written method.</p>	<p>Division with a remainder</p> <p>Short division (up to 3 digits by 1 digit)- standard written method. (concrete and pictorial if required).</p>	<p>Short division (up to 4 digits by a 1 digit number including remainders)</p>	<p>Short division</p> <p>Long division with place value counters (up to 4 digits by a 2 digit number)</p> <p>Children should exchange into the tenths and hundredths column too</p>